

Work and Energy

Work

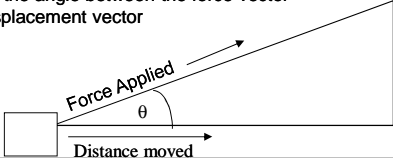
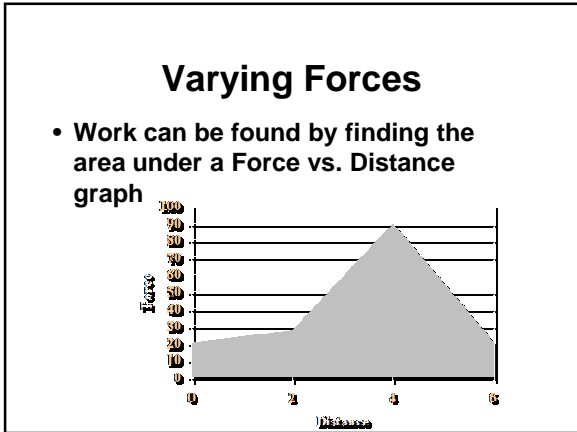
- **Definition**
 - force applied over a distance
 - distance must be in the same direction as the force
 - SI Unit of Joules
- **Equation (Linear)**
 - Work = Force x Distance
 - $W = F \times D$

Work and Direction of Force

- Work is only done if the force is exerted in the direction of motion.
- Force applied at an angle:

$$W = (F_A \cos \theta) d$$

Where θ is the angle between the force vector and the displacement vector

Varying Forces - Springs

- Any object that has an elastic property can have elastic potential energy.
- The force felt is directly proportional to the distance the object is stretched.
- This proportionality is dependent on the object itself, defined as the force constant, k. $F_{spring} = -k\Delta x$ (Hooke's Law)

$$W_{spring} = \frac{1}{2} k(\Delta x)^2$$

Energy

- **Definition**
 - The ability to do work
- **Relation of energy and work**
 - When you work, you are transferring energy to the object that you are working on.
- **Unit of Measure**
 - Joule (J)

Mechanical Energy

- (Gravitational) Potential Energy-
– energy of vertical position $U_g = mgh$
- Kinetic Energy
– Object's energy due to velocity $K = \frac{1}{2}mv^2$
- Potential Energy in a spring-
– energy of a spring based on the amount of compression or stretch

$$U_{\text{spring}} = \frac{1}{2}kx^2$$

Work-Energy Theorem

- The net work done on an object is equal to the change in its energy

$$W = \Delta K$$

Law of Conservation of Energy

- Within a closed and isolated system, energy can change form; but the total amount of energy is constant.
- Energy cannot be created or destroyed.

$$K_i + U_i = K_f + U_f$$

Classifying Forces

- Conservative
– those forces that conform the law of conservation of energy
– Ex: Gravitational, Elastic
- Dissipative
– forces that produce deviations from the law of conservation of energy
– produce forms of energy other than mechanical